

ΘΕΜΑ Α:

1 → δ, 2 → γ, 3 → γ, 4 → β Α5/ ε, λ, ε, ε, λ

ΘΕΜΑ Β:

$$B1. \quad \left. \begin{aligned} \varphi_1 &= 2\pi \left(10^{15} t - \frac{10^7}{3} x \right) \\ \varphi_1 &= 2\pi \left(\frac{t}{T_1} - \frac{x}{\lambda_1} \right) \end{aligned} \right\} \begin{aligned} 10^{15} t &= \frac{t}{T_1} \Rightarrow T_1 = 10^{-15} \text{ sec.} \\ \frac{10^7}{3} x &= \frac{x}{\lambda_1} \Rightarrow \lambda_1 = 3 \cdot 10^{-7} \text{ m.} \end{aligned}$$

• $T_2 = 2T_1$

Wien: $\lambda_1 T_1 = \lambda_2 T_2 \Rightarrow \lambda_1 T_1 = \lambda_2 \cdot 2T_1 \Rightarrow \lambda_1 = 2\lambda_2$
 $\Rightarrow \lambda_2 = \frac{\lambda_1}{2} = 1,5 \cdot 10^{-7} \text{ m.}$

$$\varphi_2 = 2\pi \left(\frac{t}{T_2} - \frac{x}{\lambda_2} \right) = 2\pi \left(\frac{t}{2 \cdot 10^{-15}} - \frac{x}{1,5 \cdot 10^{-7}} \right) \Rightarrow$$

$$\Rightarrow \varphi_2 = 2\pi \left(2 \cdot 10^{15} \cdot t - \frac{2}{3} 10^7 x \right) \text{ SI}$$

Σωστή ή

(11)

$$\begin{cases} L_1 = m \cdot v_1 \cdot R_1 \\ L_2 = m \cdot v_2 \cdot R_2 \end{cases} \Rightarrow \frac{L_1}{5L_1} = \frac{v_1 R_1}{v_2 R_2} \Rightarrow v_2 R_2 = 5 v_1 R_1$$

$$\Rightarrow v_2 \cdot \frac{m \cdot v_2}{B \cdot l \cdot v_2} = 5 \cdot v_1 \cdot \frac{m \cdot v_1}{B \cdot l \cdot v_1} \Rightarrow v_2^2 = 5 v_1^2 \quad (1)$$

$$K_1 = h \cdot f_1 - \varphi \Rightarrow \frac{1}{2} m v_1^2 = \frac{h \cdot c}{\lambda_1} - \varphi \quad (2)$$

$$K_2 = h f_2 - \varphi \Rightarrow \frac{1}{2} m v_2^2 = \frac{h \cdot c}{\lambda_2} - \varphi \quad (3)$$

$$\frac{(2)}{(3)}: \frac{v_1^2}{5 v_1^2} = \frac{\frac{h \cdot c}{2 \lambda_2} - \varphi}{\frac{h \cdot c}{\lambda_2} - \varphi} \Rightarrow \frac{h \cdot c}{\lambda_2} - \varphi = \frac{5 h c}{2 \lambda_2} - 5 \varphi$$

$$\Rightarrow 4 \varphi = 1,5 \frac{h c}{\lambda_2} \Rightarrow \varphi = \frac{1,5}{4} \cdot \frac{1250}{375} \Rightarrow$$

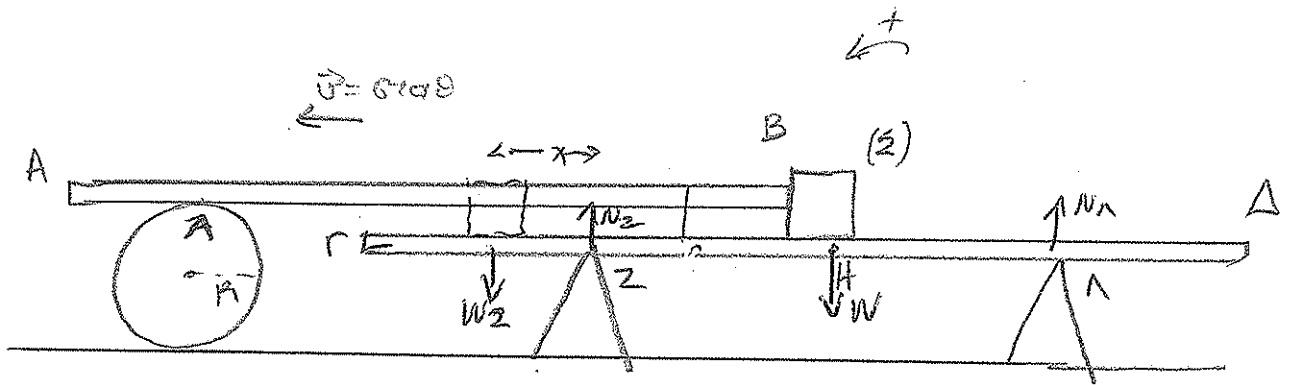
$$\Rightarrow \varphi = \frac{1,5}{4} \cdot \frac{2500}{375} = \frac{1,5 \cdot 2500}{1500} =$$

$$\Rightarrow \varphi = 2,5 \text{ eV} \rightarrow \text{Βολτα} \quad (i)$$

Σωστή η

(2)

B3)



- α)
- Ισορροπία ΓΑ: $\sum F_y = 0 \Rightarrow N_2 + N_1 = W_2 + W$ (1)
 - Στην περίπτωση $N_1 = 0$. (1) $\Rightarrow N_2 = M_2 g + M g$
 $\Rightarrow N_2 = 3Mg$ (2)
 - $\sum \tau(z) = 0 \Rightarrow W_2 \cdot x - W \cdot \frac{l}{4} = 0 \Rightarrow$
 $\Rightarrow 2Mg x = Mg \frac{l}{4} \Rightarrow x = \frac{l}{8}$ (3)
 - Άρα $d = \frac{l}{4} + \frac{l}{8} = \frac{3l}{8}$ (ii)

β) $v_1 = v \Rightarrow 2v_{cm} = v \Rightarrow v_{cm} = \frac{v}{2}$

$$\left. \begin{array}{l} x_{cm} = v_{cm} \cdot t_1 \\ x_2 = v \cdot t_1 \end{array} \right\} x_{cm} = \frac{x_2}{2} \Rightarrow x_{cm} = \frac{3l}{16}$$
 (i)

(3)

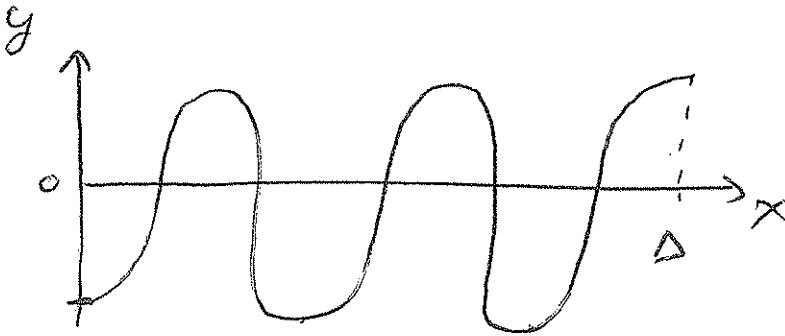
ΘΕΜΑ Γ

Γ1) 60 φορές από θ1 → N = 30 ΕΛΑΝΟΑ. σε Δt = 60 sec

$$f = \frac{N}{\Delta t} = \frac{30}{60} = 0,5 \text{ Hz}, \quad T = \frac{1}{f} = 2 \text{ sec.}$$

$$\omega = \frac{2\pi}{T} = \pi \text{ rad/s}$$

$$x_{\Delta} = 2,5 \text{ m}$$



$$x_{\Delta} = 2,5 \lambda \Rightarrow \lambda = 1 \text{ m}, \quad v_s = \lambda \cdot f = 0,5 \text{ m/s.}$$

$$t_{\Delta} = 2,5 T \quad \text{Άρα} \quad 2 \text{ m} = 10 A \Rightarrow \underline{\underline{A = 0,2 \text{ m}}}$$

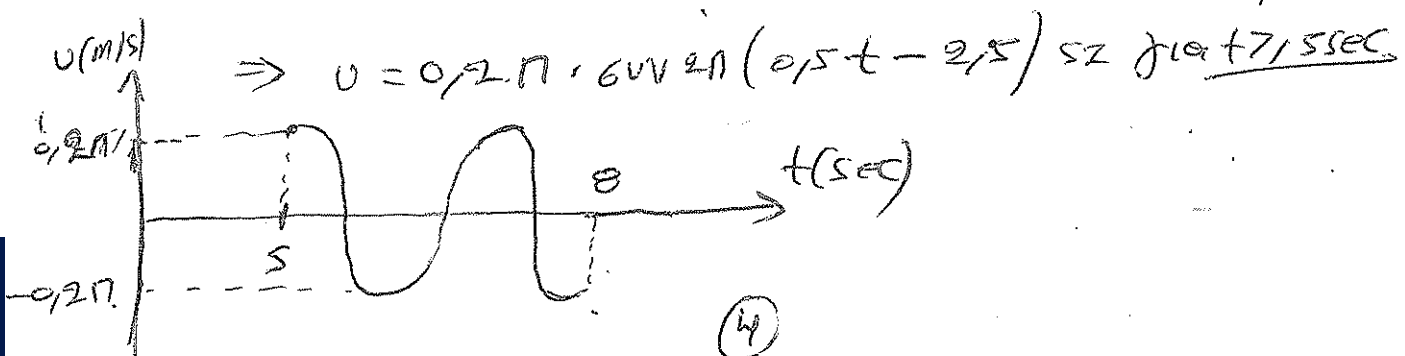
Γ2) Το σήμα Δ ξεκινάει την t_Δ :

Μια τυχαία στιγμή t θα ταλαντώνεται για t - t_Δ
 $\Rightarrow t - \frac{x_{\Delta}}{v_s}$

$$y = A \cdot \eta \psi \left(t - \frac{x_{\Delta}}{v_s} \right) = A \cdot \eta \psi \frac{2\pi}{T} \left(t - \frac{x_{\Delta}}{v_s} \right) \Rightarrow y = A \cdot \eta \psi \left(2\pi \left(\frac{t}{T} - \frac{x_{\Delta}}{\lambda} \right) \right)$$

Γ3) t_Δ = 2,5 T = 5 sec

$$u_{\Delta} = u_{\text{max}} \cdot \cos 2\pi \left(\frac{t}{T} - \frac{x_{\Delta}}{\lambda} \right) = 0,2\pi \cdot \cos 2\pi \left(\frac{t}{2} - \frac{2,5}{1} \right)$$



Γ4) Συμφωνία φάσης:

$$\Delta x = k \cdot \lambda \Rightarrow 2,5 = 2 \Rightarrow \underline{\lambda = 2,5 \text{ m}} \quad (\text{ή } \lambda' = 2,5 \text{ m})$$

$$v = \lambda \cdot f \Rightarrow f' = \frac{v}{\lambda'} = \frac{0,5}{2,5} = \frac{1}{5} = 0,2 \text{ Hz}$$

$$\text{Άρα } \Delta f = f' - f = -0,3 \text{ Hz}$$

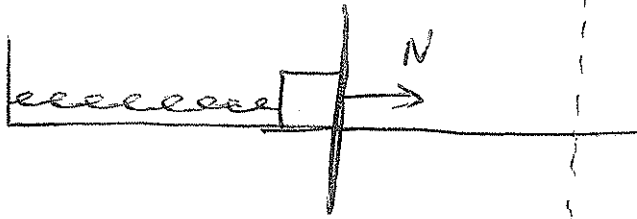
ΦΡΟΝΤΙΣΤΗΡΙΑ ΣΥΣΤΗΜΑ ΠΥΛΑΙΑΣ-ΠΑΝΟΡΑΜΑΤΟΣ-ΧΟΡΤΙΑΤΗ

5

ΘΕΜΑ Δ

ΘΙ, ΦΜ

Δ1)



α)

Για φάση δ: $\sum F_x = m_p a \Rightarrow N = m_p \omega^2 x \Rightarrow x = 0$ (with $N=0$ above the equation)

β) Αρχικά: $\omega = \sqrt{\frac{k}{m_p + m}} = 2,5 \text{ rad/s}$

Στην ΘΙ/ΦΜ: $v_k = v_{\max} = \omega \cdot A = \omega \cdot \Delta\phi = 1 \text{ m/s}$

Μετά το χορήγιο ενοποίησης:

$v_{\max}' = v_{\max} = \omega' \cdot A' \quad \text{①}$

$\omega' = \sqrt{\frac{k}{m_s}} = 5 \text{ rad/s}$

① $\Rightarrow A' = 0,2 \text{ m}$

Δ2) Κίνηση ΛΜ $\rightarrow \Delta\phi \dots \rightarrow \Sigma \epsilon \epsilon \eta \quad t \in \Lambda(A), \mu(-)$

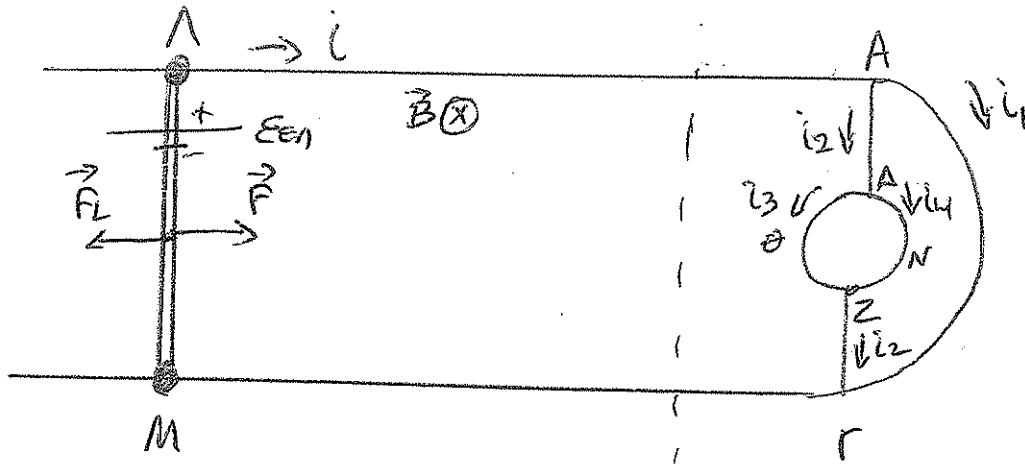
(ή $F_{\text{εστρε}} \leftarrow \text{ενδ} \Lambda \text{Μ προς } \Lambda$)

Δ3) $\sum F = m_p \cdot a \Rightarrow F = m_p \cdot a \Rightarrow a = 2,5 \text{ m/s}^2$

$v = v_{\max} + a \cdot (t_2 - t_1) \Rightarrow v = 6 \text{ m/s}$

6

Δ4)



a)

$$R_{ANZ} = R_{\Delta\theta Z} = \frac{R_2}{2} = 5\Omega$$

$$R_{ANZ} \parallel R_{\Delta\theta Z} : R_{ANZ, \Delta\theta Z} = \frac{R_{ANZ} \cdot R_{\Delta\theta Z}}{R_{ANZ} + R_{\Delta\theta Z}} = 2,5\Omega$$

$$R_{07} = \frac{R_{ANZ, \Delta\theta Z} \cdot R_1}{R_{ANZ, \Delta\theta Z} + R_1} = 2\Omega$$

$$\text{Ohm: } i = \frac{\varepsilon E_{\text{eff}}}{R_{07}} = \frac{B \cdot v \cdot l}{R_{07}} = 3\text{A}$$

$$\text{Σωενως: } F_L = B \cdot i \cdot l = 3\text{N}$$

$$\text{Αρα: } \Sigma F = F - F_L = 0 \Rightarrow v = 6 \text{ τα δευτ } \Rightarrow \text{ΕΟΚ}$$

$$b) i = \frac{V_{\text{eff}}}{R_1} = \frac{\varepsilon E_{\text{eff}}}{R_1} = \frac{6}{10} = 0,6\text{A}$$

$$\text{Ισως KK: } i = i_2 + i_1 \Rightarrow i_2 = i - i_1 \Rightarrow i_2 = 2,4\text{A}$$

$$V_{\Delta\theta 2} = V_{\Delta\omega 2} \Rightarrow i_3 R_{\Delta\theta 2} = i_4 R_{\Delta\omega 2} \Rightarrow i_3 = i_4$$

$$i_{\text{ολ}} = i_2 = i_3 + i_4 \Rightarrow i_2 = 2i_3 \Rightarrow i_3 = \frac{i_2}{2} = \frac{1,2\text{A}}{2} = 0,6\text{A} = i_4$$

$$\Delta 5) \text{ α)} \quad dB_1 = \frac{\mu_0}{4\pi} \cdot \frac{i_1 \cdot d\ell}{r_1^2} \cdot \sin 90^\circ = \frac{\mu_0}{4\pi} \frac{i_1 \cdot d\ell}{r_1^2} \quad (1)$$

$$B_1 = \int dB_1 = \frac{\mu_0}{4\pi} \cdot \frac{i_1}{r_1^2} \int d\ell = \frac{\mu_0}{4\pi} \frac{i_1}{r_1^2} \frac{2\pi r_1}{1} \Rightarrow$$

$$\Rightarrow B_1 = \frac{\mu_0}{4\pi} \cdot \frac{\pi i_1}{r_1} \Rightarrow B_1 = 12\pi \cdot 10^{-8} \text{T} \quad \mu \in \vec{B}_1 \otimes$$

$$\text{β)} \quad dB_{\Delta\theta 2} = \frac{\mu_0}{4\pi} \frac{i_3 \cdot d\ell}{r_2^2} \cdot \sin 90^\circ \quad \mu \in dB_{\Delta\theta 2} \ominus$$

$$dB_{\Delta\omega 2} = \frac{\mu_0}{4\pi} \frac{i_4 \cdot d\ell}{r_2^2} \cdot \sin 90^\circ \quad \mu \in dB_{\Delta\omega 2} \otimes$$

$$\text{Συνεπώς: } \vec{B}_{\text{συνολικό}} = dB_{\Delta\theta 2} + dB_{\Delta\omega 2} = 0$$

$$\text{Άρα } \vec{B}_{\text{ολ}} = \vec{B}_1 \Rightarrow |B_{\text{ολ}}| = |B_1| = 12\pi \cdot 10^{-8} \text{T}$$

$\mu \in \vec{B}_1 \otimes$ δηλ. $\mu \in$ φορά έξω των αναγωγών στην εφεξής διατμήση.